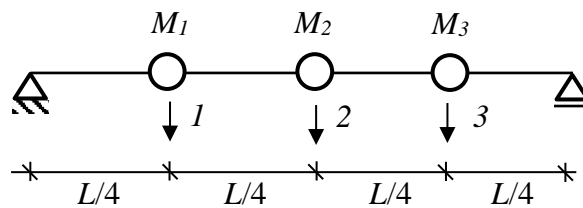




### EXERCÍCIO PARA A VF #1

Para o sistema estrutural a seguir, pede-se:

- Mostre que se  $[K] = [F]^{-1}$ , então  $\left\{ \frac{1}{\omega^2} I - [F][M] \right\} \phi = 0$ ;
- As frequências naturais, em Hz;
- As formas modais (vetores normalizados e esboço).



$$EI = 2 \cdot 10^4 \text{ kNm}^2 \quad L = 12 \text{ m} \quad M_2 = 0,75 \cdot M_1 = 0,75 \cdot M_3 = 1.000 \text{ kg}$$

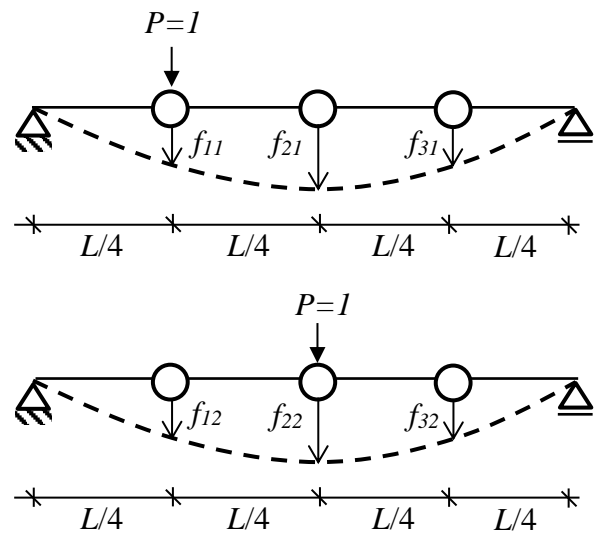
$$[F] = \begin{bmatrix} f_{11} & f_{12} & f_{13} \\ f_{21} & f_{22} & f_{23} \\ f_{31} & f_{32} & f_{33} \end{bmatrix}$$

$$f_{11} = f_{33} = \frac{9}{768} \cdot \frac{L^3}{EI}$$

$$f_{13} = f_{31} = \frac{7}{768} \cdot \frac{L^3}{EI}$$

$$f_{12} = f_{21} = f_{32} = f_{23} = \frac{11}{768} \cdot \frac{L^3}{EI}$$

$$f_{22} = \frac{16}{768} \cdot \frac{L^3}{EI}$$



### FORMULÁRIO - Problema de Autovalor-Autovetor:

$$\{ [K] - \omega^2 [M] \} \phi = 0$$

$$\{ [M]^{-1} [K] - \omega^2 I \} \phi = 0$$